

TABLE VI

<sup>*a*</sup> The a-b pairs are enantiomers.  $\bar{b}$  Reference 11. *c* A denotes an apex-equatorial pair. E denotes a pair in the same equatorial ring, and E' denotes *a* pair which has one member in each ring. <sup>d</sup> In Hermann-Mauguin and Schoenflies notations, respectively.

which may be so constructed, five of which are symmetric and the remaining eight of which form four enantiomorphic pairs. Other isomers involving bridging to nonadjacent atoms were not considered because of the drastic crowding of the pair of B-H groups which lie between any such nonadjacent pair. The thirteen isomers are listed in Table VI, together with the point groups to which they belong and an indication of which pairs of atoms in each polyhedron are involved in the hydrogen bridges. The isomer found in this investigation is the fifth listed in Table VI, while no. 1 was proposed<sup>10</sup> for the structure of the parent  $B_{20}H_{18}^2$ <sup>-</sup> ion before it was shown<sup>6,7</sup> to be linked by a pair of B-B-B three-center bonds rather than hydrogen bridges. Hawthorne and Pilling mention<sup>3</sup> "the formation of unidentified metastable intermediates" in the thermal reversion of the photoisomer studied here to the parent ion. Thus it may be that some or all of the isomers discussed here also exist.

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# Structure of Gadolinium Sesquisulfide

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The structure of  $Gd_2S_3$  has been solved and refined by least-squares procedures to an *R* of 0.019 using 540 nonequivalent reflections collected with a counter diffractometer. Crystals were grown in a GdI<sub>3</sub> melt at 1200°. The crystals are orthorhombic with  $a = 7.339$  Å,  $b = 15.273$  Å,  $c = 3.932$  Å,  $D_m = 6.14$  g cm<sup>-3</sup>,  $D_x = 6.187$  g cm<sup>-3</sup> for  $Z = 4$ , and space group Pnam. Two kinds of nonequivalent gadolinium atoms are present in Gd<sub>2</sub>S<sub>3</sub>. One is surrounded by a monocapped trigonal prism of sulfur atoms while the other gadolinium atom is in a bicapped trigonal prism of sulfur atoms. This structure is found for rare earth sesquisulfides from La through Dy and probably also for  $Pu_2S_3$ .

### Introduction

Very little structural information has been available on rare earth sesquisulfides. (Rare earths will be considered to be La through Lu plus *Y* and Sc.) The structure of  $Sc_2S_3$ , determined by Dismukes and White,<sup>1</sup> is related to the NaCl structure. Apparently, this structure exists for certain rare earth sesquiselenides and sesquitellurides<sup>2,3</sup> but not for any other rare earth sesquisulfide.

According to Flahaut, $4$  there are five possible structures for the rare earth sesquisulfides other than that of Sc<sub>2</sub>S<sub>3</sub>. Two rare earth sulfides,  $Yb_2S_3$  and  $Lu_2S_3$ , have the corundum structure.<sup>5</sup> Five-Dy<sub>2</sub>S<sub>3</sub>, Y<sub>2</sub>S<sub>3</sub>, Er<sub>2</sub>S<sub>3</sub>,  $H_0S_3$ , and  $Tm_2S_3$ —have a monoclinic structure. Sesquisulfides from La through Tb can have a defect

 $Th_3P_4$ -type structure which actually exists over a range of compositions. In addition, Flahaut<sup>4</sup> stated, mainly on the basis of powder patterns, that there are two unknown structures which are referred to as *a*  and  $\beta$  types. A comparison of the powder pattern of Nd2S3 reported by Picon, *et al.,6* with a powder pattern of our  $Gd_2S_3$  crystals indicated that our crystals are of the general  $\alpha$ -sesquisulfide structure type. Since this structure has been found for sesquisulfides of La through  $Dy^7$  and also for  $Pu_2S_3^s$  and since suitable single crystals were prepared for the first time, an investigation of the  $Gd_2S_3$  structure was undertaken.

### Experimental Section

Synthesis.--Crystal sponge gadolinium metal  $(99.9\%)$  was obtained from the Lunex Co. Sulfur was  $99.999\%$ , and iodine was reagent grade resublimed. The three reactants were sealed

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<sup>(1)</sup> J. P. Dismukes and J. G. White, *1;toug. Chem.,* **8,** 1220 (1964).

**<sup>(2)</sup>** J. P. Dismukes and J. G. White, *ibid.,* **4,** 970 (1965).

**<sup>(3)</sup>** J. Flahaut, I,. Pierre, M. Pardo, and M. Guittard, *Rid. .SOC. Chiin. Fyance,* 1399 (1965).

<sup>(4)</sup> J. Flahaut, M. Guittard, *hl.* Patrie, M. P. Pardo, S. **Ivf.** Golabi, and L. Domange, *Acte Cryst.,* **19, 14 (1965).** 

*<sup>(5)</sup>* J. Flahaut, L, Domange, and **M.** Pardo, *Compf. Rend.,* **268,** 594 (1964).

<sup>(6)</sup> M. Picon, L. Domange, J. Blahaut, M. Guittard, and M. Patrie, *Bull.* SOC. *Chim Fvaiace,* 221 (1960).

**<sup>(7)</sup> A.** W. Sleight, to **be** submitted for publication,

<sup>(8)</sup> J. P. Marcon and 11. Pascard, *J. Inoug. Nud. Chem.,* **28,** 2551 (1966).

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283 279<br>691 693<br>697 501<br>1184 1194



TABLE I

*a* For each set of fixed *k* and *l*, the columns are *h*,  $10F_0$ , and  $10F_0$ . Unobserved reflections and those for which the secondary extinction correction was greater than  $25\%$  are marked by an asterisk and E, respectively.

in an evacuated silica ampoule in an atomic ratio of  $1:1:1$ . The ampoule was heated very slowly to avoid a violent reaction which can cause considerable container attack as well as frequent failure. After the reaction was complete, possibly forming GdSI, the temperature was raised to 1200" for about 20 hr.

After the ampoule was cooled to room temperature and opened, red needle-like crystals of  $Gd_2S_3$  were found along with  $GdI_3$ . The GdI<sub>3</sub> was washed away with water. Although the odor of H<sub>2</sub>S was present, the crystals of  $Gd_2S_3$  were relatively unaffected by the washing. This method of crystal preparation has been found generally applicable for rare earth sesquisulfides.<sup>7</sup> Anal. Calcd for Gd<sub>2</sub>S<sub>3</sub>: Gd, 76.6; S, 23.4. Found: Gd, 76.4; S, 22.2. Iodine was undetectable by X-ray fluorescence.

X-Ray Data.--For Gd<sub>2</sub>S<sub>3</sub> the formula weight is 410.68 and *a*  $= 7.339 \pm 7 \text{ Å}, b = 15.273 \pm 2 \text{ Å}, \text{ and } c = 3.9318 \pm 4 \text{ Å}.$ The least-squares refinement of deWolff-Guinier photograph data was done at  $25^\circ$ . High-purity KCl  $(a = 6.29310 \text{ Å})$ , obtained from Johnson, Matthey & Co., was used as an internal standard. For the crystal we have:  $V = 440.70 \pm 5 \text{ Å}^3$ ;  $D_m = 6.14 \pm 5$  g cm<sup>-3</sup> (displacement method);  $Z = 4$ ;  $D_x$  $= 6.187 \text{ g cm}^{-3}$ ;  $\mu = 167 \text{ cm}^{-1}$  (Ag Ka). Approximate crystal dimensions are:  $0.0034 \times 0.0067 \times 0.04$  cm, with the longest dimension parallel to **c.** The space group is Pnam- $D_{2h}^{16}$  or  $Pna2_1-C_{2v}^{9}$  (absences, from precession photographs: *Okl,*  $k + l \neq 2n$ *; hOl,*  $h = 2n$ *).* The space group Pnam was confirmed by the absence of piezoelectric effect, by examination of Patterson maps, and by analysis of refinement results.

### Structure Solution and Refinement

Three-dimensional diffraction intensities were measured with a Picker automatic diffractometer using Pd-filtered Ag  $K\alpha$  radiation at a take-off angle of  $3^\circ$ and a scintillation detector. Reflections were scanned for 1.5° plus the  $\alpha_1-\alpha_2$  dispersion, and 40-sec backgrounds were measured at the extremes of each scan. The half-maximum width of the 020 reflection  $(2\theta = 4.21^{\circ})$  was 0.28°, thus indicating that the mosaicity of the crystal is relatively small. In making background corrections, a linear background dependence between each extreme was assumed. Prismatic crystal absorption corrections resulting in transmission factors varying from 0.41 to 0.67 were computed

using the method of Wuensch and Prewitt.<sup>9</sup> In all, 567 reflections in one octant of reciprocal space were recorded. Several medium to strong sets of symmetryequivalent reflections were checked to see that they were equivalent in intensity; however, no statistical studies were made of these sets. The maximum  $2\theta$ was  $43^\circ$ .

.L= 5, k<br>- 964 - 966<br>- 859 - 857<br>- 814 - 807

From three-dimensional Pattersons maps, the locations of two nonequivalent gadolinium atoms were determined, assuming space group Pnam. A subsequent electron density map computed with signs determined by  $Gd(1)$  and  $Gd(2)$  was sufficient to locate  $S(1)$ ,  $S(2)$ , and  $S(3)$ . All atoms lie on mirror planes in equipoint 4c  $(x, y, \frac{1}{4}; \bar{x}, \bar{y}, \frac{3}{4}; \frac{1}{2} - x, \frac{1}{2} + y,$  $\frac{3}{4}$ ;  $\frac{1}{2} + x$ ,  $\frac{1}{2} - y$ ,  $\frac{1}{4}$ ). A few cycles of refinement with a full-matrix, least-squares program  $SFLS5^{10}$  in<br>which  $\sum w \left| \begin{bmatrix} F_0 \\ F_1 \end{bmatrix} \right| = \left| \begin{bmatrix} F_0 \\ F_1 \end{bmatrix} \right|^{2}$  was minimized, reduced which  $\sum w||F_0|$  –  $|F_0||^2$  was minimized, reduced <br> *R* (*R* =  $\sum ||F_0|$  –  $|F_0||/\sum |F_0|$ ) to 0.06. *σ* terms for

$$
\sigma_{F_0} = (Lp)^{-1/2}[(I + \sigma_I)^{1/2} - I^{1/2}]
$$

where  $L$ ,  $p$ , and  $T$  are the Lorentz, polarization, and transmission factors, respectively, *I* is the integrated intensity, and

$$
\sigma_I = \left[ E + \left( \frac{T_E}{2T_B} \right)^2 (B_1 + B_2) + \epsilon^2 I^2 \right]^{1/2}
$$

Here *E* is the total count plus background,  $T<sub>B</sub>$  and  $T<sub>B</sub>$ are peak and background times, *B1* and *Bz* are background counts, and *E,* set in this case to 0.03, accounts for fluctuations in the direct beam and other uncertainties.

Further refinement in which the anisotropic temperature factors and the secondary-extinction parameter  $C^{11,12}$   $[C = 0.219(8) \times 10^{-5}]$  were varied

**<sup>(9)</sup>** B. **J. Wuensch and** *C.* **T. Prewitt,** *Z. Kvist.,* **199, 24 (1905).** 

<sup>(10)</sup> C. T. **Prewitt, unpublished computer program.** 

**<sup>(11)</sup> VI. H. Zachariasen,** *Acta Crysf.,* **16, 1139 (1963).** 

<sup>(12)</sup> *C.* T. **Prewitt and R. D. Shannon,** *ibid.,* **in press.** 



TABLE **I1** 

**<sup>a</sup>**Points at the left of each decimal entry are omitted.

reduced *R* to 0.019 and *wtdR* to 0.027 for 540 reflections included in the refinement. Excluded were **3** strong reflections for which the extinction correction was greater than  $25\%$  and 24 unobserved reflections. If the 3 strong reflections are included, *R* increases to 0.020. The standard deviation of an observation of unit weight was 1.50. Table I gives the final observed and calculated structure factors. Form factors for neutral Gd and S were taken from Cromer and Waber.<sup>13</sup> Real and imaginary anomalous dispersion factors for Ag K $\alpha$  radiation from Cromer<sup>14</sup> were applied in the usual way.

Atomic coordinates and anisotropic temperature factors are listed in Table 11. Interatomic distances and angles plus the magnitudes and orientations of the thermal ellipsoid were calculated<sup>15</sup> and are given in Figures 1 and *2* and Table 111.



**MAGNITUDES AND ORIENTATIONS OF THERMAL ELLIPSOIDS** 



### Discussion

Figures 1 and 3 are diagrams of the  $Gd_2S_3$  structure. Figure 1 shows the bonds and atom positions, and Figure 3 is a stereographic view. The structure is composed of GdS<sub>7</sub> and GdS<sub>8</sub> polyhedra which are linked in a complex way to form a three-dimensional structure. The coordination of Gd(1) is by eight sulfur atoms in a bicapped trigonal prism at average distances of  $2.90 \text{ Å}$ , and  $Gd(2)$  is coordinated by seven sulfur atoms in a distorted monocapped trigonal prism at average distances of 2.82 **8.** A capped trigonal prism arrangement seems to be a common coordination

**(14)** D. T. Cromer, *ibid.,* **18,** 17 (1965). **(15)** W. R. **Busing,** K. 0. Martin, and H. **A.** Levy, ORNL-TN-305, **Oak**  Ridge National Laboratory, Oak Ridge, Tenn., 1962.



Figure 1.—Model of the  $Gd_2S_3$  structure,



Figure 2.-Coordination polyhedra around (a)  $Gd(1)$ , (b) Gd(2), (c) S(1), (d) S(2) and S(3). The lengths of the polyhedral edges are the S-S distances in (a) and (b) and the Gd-Gd distances in (c) and (d). In (d), the values corresponding to S(2) are given first. The vertical edges of the polyhedra are all equal to  $c, i.e., 3.932 \text{ Å}.$ 



Figure 3.-Stereographic view of the  $Gd_2S_3$  structure.

for rare earths and actinides. In  $Sm<sub>2</sub>O<sub>8</sub>$  (B rare earth sesquioxide structure) there are monocapped trigonal prisms.16 Many rare earth and actinide halides have the PuBr<sub>3</sub> structure,<sup>17</sup> which has bicapped trigonal prisms. The rare earth coordination in LaTe<sub>2</sub> and

**<sup>(13)</sup>** D. T. Cromer and **J.** T. Waber, *Acta Cyyst.,* **18, 104** (1965).

<sup>(16)</sup> D. T. Cromer, *J. Phys. Chem.,* **61,** 753 (1957).

<sup>(17)</sup> W. H. Zachariasen, Acta Cryst., **1, 266** (1948).

 $NdTe<sub>2</sub><sup>18</sup>$  may be described as a tricapped trigonal prism.

The sulfur atoms in  $Gd_2S_3$  are all coordinated by five gadolinium atoms. A trigonal-bipyramidal arrangement is found for S(1) with average S-Gd distances of 2.90 Å, and  $S(2)$  and  $S(3)$  are in square pyramids with average S-Gd distances of 2.85 and 2.83 A, respectively. Figure 2 shows the coordination polyhedra associated with each atom. The S-S distances are all greater than 3.40 Å except for one of  $3.04$  Å between  $S(2)$  and  $S(3)$ centered around the point 0.37, 0.48,  $\frac{3}{4}$  in Figure 1. This short *S(2)-S(3)* distance represents a polyhedral edge shared between two Gd(1) polyhedra and one Gd(2) polyhedron and is the only edge shared by more than two of the gadolinium polyhedra. There are, however, no unusually short Gd-Gd distances in the

(18) R. Wang, H. Steinfink, and W. F. Bradley, *Inorg. Chem.*, 5, 142 (1966).

structure, the shortest being one of 3.888 A between  $Gd(1)$  and  $Gd(2)$ . This is consistent with the magnetic data7 which indicate very weak interactions between gadolinium atoms. For  $Gd_2S_3$  there are no magnetic transitions down to 4.2'K, the Curie-Weiss constant  $(\theta)$  is  $-8^{\circ}K$ , and the observed moment of  $7.94 \pm 0.01$  BM is in excellent agreement with the calculated value19 of 7.94 BM.

Recently, a structure for monoclinic  $Ho<sub>2</sub>S<sub>3</sub>$  has been reported<sup>20</sup> which contains half of the Ho in octahedral and half in sevenfold coordination. Thus the coordination of the rare earth is showing a general tendency to increase as the size of the rare earth increases, going from six in the corundum type, through mixed six and seven in the monoclinic type, to mixed seven and eight in the orthorhombic type.

(19) J. H. Van Vleck, "The Theory of Electric and Magnetic Susceptibili- (20) **J.** G. White, P. N. Yocom, and S. Lerner, *Inorg. Chem., 6,* 1872 (1967).

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# Magnetic, Mössbauer, and Structural Studies on Three Modifications of FeMoO<sub>4</sub>

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Three modifications of FeMoO<sub>4</sub> have been characterized by magnetic susceptibility, Mössbauer effect, and X-ray studies. The low-temperature, low-pressure form,  $\alpha$ -FeMoO<sub>4</sub>, is isostructural with low-temperature NiMoO<sub>4</sub> and CoMoO<sub>4</sub>. The high-temperature, low-pressure form,  $\beta$ -FeMoO<sub>4</sub>, is isostructural with MnMoO<sub>4</sub> and MgMoO<sub>4</sub> and exists metastably at room temperature when quenched from above 600". The high-pressure form, FeMo04-11, represents a triclinic distortion of the monoclinic NiWO4-type structure. Magnetic and Mossbauer results indicate high-spir divalent iron to be present in all three modifications. Antiferromagnetic interactions in FeMo04-I1 lead to magnetic order below **45°K.** 

### Introduction

At least two forms of  $FeMoO<sub>4</sub>$  are known to exist. A low-pressure modification,  $\alpha$ -FeMoO<sub>4</sub>, was first prepared by Schultzel as monoclinic prisms from a fusedsalt reaction. This product has also been reported by others, $2-6$  and the X-ray diffraction powder pattern has been presented. $2,6,7$  Its structure has generally been believed to be different from those of the normal (STP) forms of all other  $A^{2+}Mo^{6+}O_4$ -type molybdates (where A may be Mg, Mn, Co, Ni, Zn, and  $Cu$ ).<sup>8-10</sup> Abrahams<sup>11</sup> states that normal (STP) FeMo $O<sub>4</sub>$  is

(1) H. Schultze, Ann., **126,** 49 (1863).

(2) Yu. D. Kozmanov, Zh. Fiz. Khim., 31, 1861 (1957).

(3) A. N. Zelikman and L. V. Belyaevskaya, *Zh. Prikl. Khim., 27,* 1151 (1954); **29,** 11 (1956).

(4) A. N. Zelikman, *Zh. Neorgan. Khim.,* **1,** 2778 (1956). *(5)* Yu. D. Kozmanov and T. A. Ugol'nikova, *ibid.,* **3,** 1267 (1958).

(6) W. Jäger, A. Rahmel, and K. Becker, *Arch. Eisenhuttenw.*, 30, 435 (1959).

- (7) *F.* Corbet, R. Stefani, J. C. Merlin, and C. Eyrand, *Comfit. Rend.,* **246,**  1696 (1958).
- (8) G. W. Smith and J. A. Ibers, *Acta Ct'yst.,* **19,** 269 (1965).
- (9) G. W. Smith, *ibid.,* **15,** 1054 (1962).
- (10) S. C. Abrahams and **J.** M. Reddy, J. *Chem. Phys., 43,* 2533 (1965).

(11) **S.** C. Abrehams, *ibid.,* **46,** 2052 (1967).

probably triclinic. Young and Schwartz<sup>12</sup> have reported a high-pressure modification,  $FeMoO<sub>4</sub>-II$ , which they found to be structurally related to  $NiWO<sub>4</sub>$ .

The purpose of this investigation was to identify the various modifications of  $FeMoO<sub>4</sub>$  and to compare their properties. It was of particular interest to determine if the reportedly unique structure for  $\alpha$ -FeMoO<sub>4</sub> might be due to an unusual valence combination, *i.e.,* Fe3+-  $Mo<sup>5+</sup>O<sub>4</sub>$ , instead of  $Fe<sup>2+</sup>Mo<sup>6+</sup>O<sub>4</sub>$ .

### Experimental Section

All forms of FeMoO4 could be prepared from an appropriate mixture of  $Fe<sub>2</sub>O<sub>8</sub>$ , MoO<sub>3</sub>, and Mo or  $Fe<sub>2</sub>O<sub>8</sub>$ , MoO<sub>3</sub>, and Fe. The reactants, obtained from Johnson, Matthey & Co., were all at least  $99.99\%$  pure. Both low-pressure forms of FeMoO<sub>4</sub> were prepared by heating the intimately mixed reactants in evacuated platinum or silica tubes at 900-1000' for **1-2** days. Depending on the cooling rate, the product was  $\alpha$ -FeMoO<sub>4</sub>,  $\beta$ -FeMoO<sub>4</sub>, or a mixture of these two forms.  $\alpha$ -FeMoO<sub>4</sub> was also prepared by mixing stoichiometrically solutions of FeCl<sub>2</sub> and Na<sub>2</sub>MoO<sub>4</sub> at about 100° and then drying the precipitate at 400° under vacuum.

<sup>(12)</sup> A. P. Young and C. M. **Schwartz,** Science, **141,** 348 (1963).